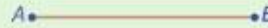


**Construct an angle of 60 degrees with a protractor**

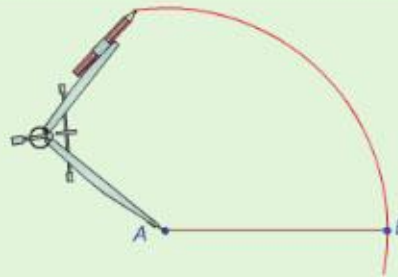
Construct an angle of  $60^\circ$  without using a protractor or a set square.

**Solution**

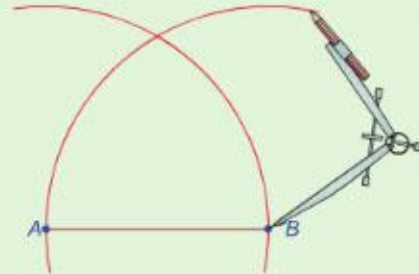
Draw a line segment  $[AB]$ .



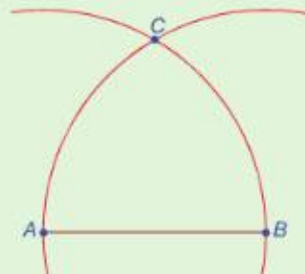
Place the compass point at  $A$ , and draw an arc of radius length  $|AB|$ .



Place the compass point at  $B$ , and draw an arc of radius length  $|AB|$ .

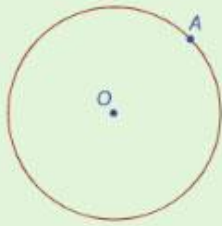


Mark the point of intersection of the arcs and label as point  $C$ .



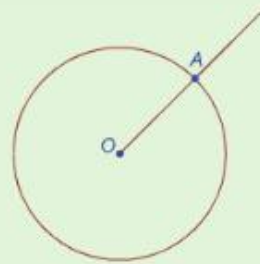
## Tangent to a circle at a given Point

Construct a **tangent** to the given circle at the point A.

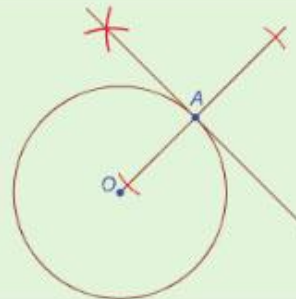


A **tangent** is a line that touches the circle at a single point.

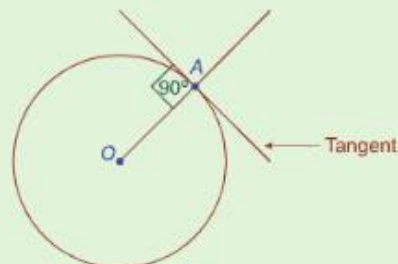
Draw a ray from the centre O of the circle through the given point A.



Construct a line perpendicular to the ray [OA through the point A.

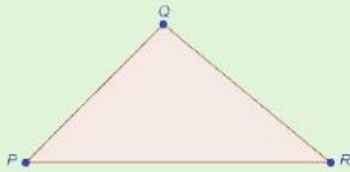


This is the tangent to the circle.

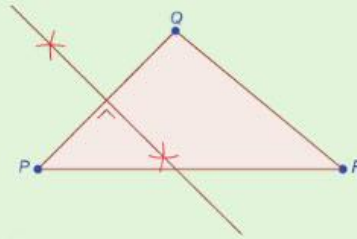


# The Centroid of a Triangle

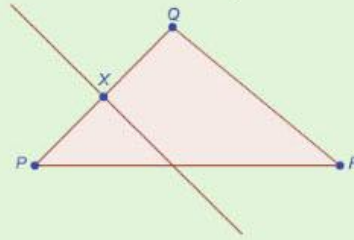
Construct the centroid of the triangle  $PQR$ .



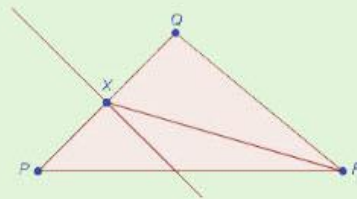
Construct the perpendicular bisector of the side  $[PQ]$ .



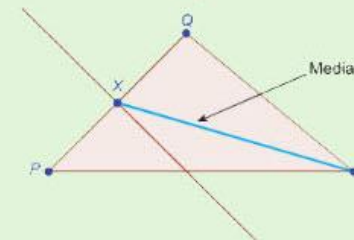
Label the midpoint of  $[PQ]$  as the point  $X$ .



Using a straight edge, draw a line from  $X$  to  $R$ , the opposite vertex of the triangle.

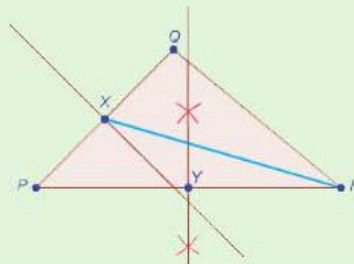


This line is a **median** of the triangle  $PQR$ .



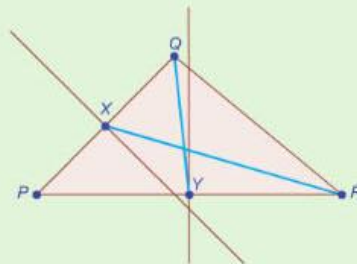
A **median** of a triangle is a segment that goes from one of the triangle's vertices to the midpoint of the opposite side.

Construct the perpendicular bisector of  $[PR]$  and label the midpoint  $Y$ .

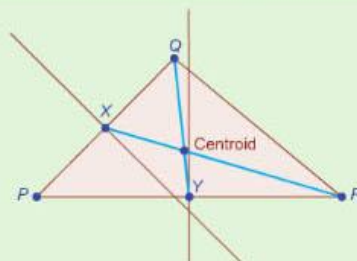


Using a straight edge, join  $Y$  to the opposite vertex,  $Q$ .

This is a second median.



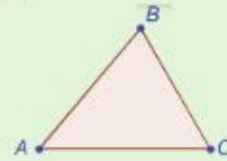
Where the medians intersect is the centroid of the triangle  $PQR$ .



The **centroid** is the triangle's balance point or centre of gravity, i.e. the point where the three medians of the triangle meet.

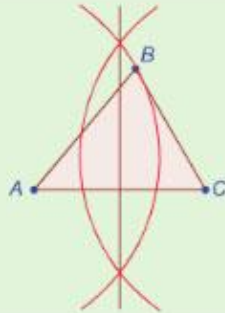
## Circumcentre and Circumcircle

Construct the circumcentre and circumcircle of the triangle  $ABC$ .

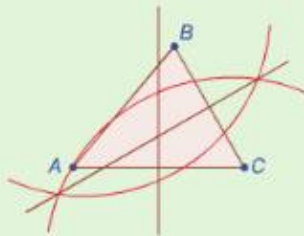


### Solution

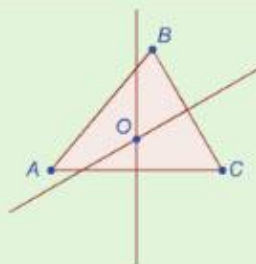
Construct the perpendicular bisector of  $[AC]$ .



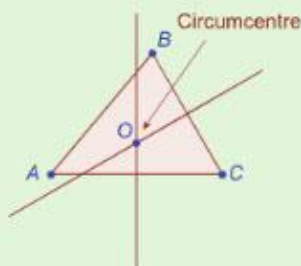
Construct the perpendicular bisector of any other side of the triangle – in this case the side  $[BC]$ .



Mark the point of intersection of the perpendicular bisectors and label as point  $O$ .

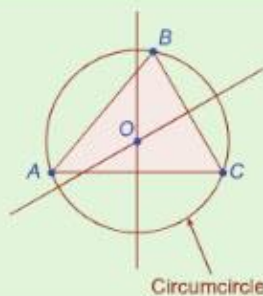


Point  $O$  is the **circumcentre** of the triangle  $ABC$ .



The **circumcentre** is the point where a triangle's three perpendicular bisectors meet.

Place the compass point on  $O$  and draw a circle of radius length  $|OA|$ . This circle is the **circumcircle** of the triangle  $ABC$ .

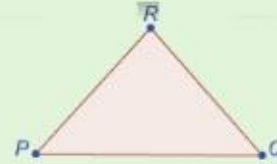


The **circumcircle** of a triangle is a circle that passes through all three vertices of the triangle.



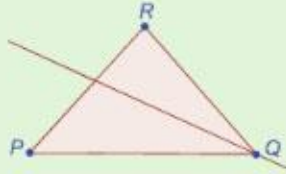
## Incentre and Incircle of a Triangle

Construct the incentre and incircle of the triangle  $PQR$ .

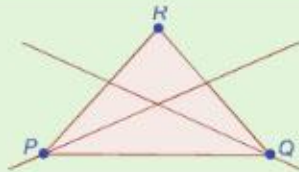


### Solution

Construct the bisector of the angle  $PQR$ .

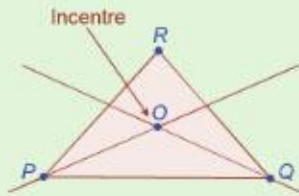


Construct the bisector of any other angle in the triangle, e.g.  $\angle RPQ$ .



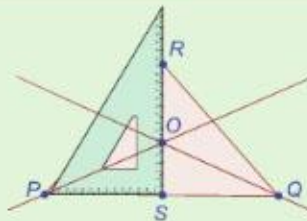
Mark the point of intersection of the angle bisectors, and label as point  $O$ .

Point  $O$  is the **incentre** of the triangle  $PQR$ .



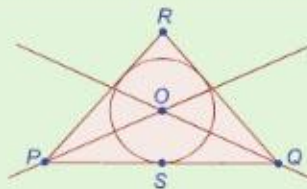
The **incentre** is the point where a triangle's three angle bisectors meet.

Using your set square, draw a perpendicular from  $O$  to a side of the triangle. Label the point where it meets this side as  $S$ .



Place the compass point on  $O$  and the pencil on  $S$ , and draw a circle. This circle should touch all three sides of the triangle.

This is the **incircle** of the triangle  $PQR$ .



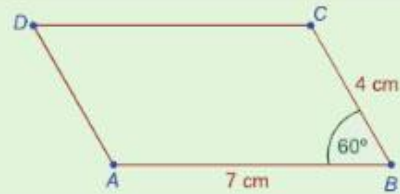
The **incircle** of a triangle is the largest circle that will fit inside the triangle. Each of the triangle's three sides is a tangent to the circle.

## Parallelogram of given side lengths and given Angle

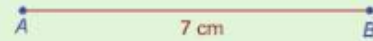
Construct a parallelogram  $ABCD$  where  $|AB| = 7$  cm,  $|BC| = 4$  cm and  $|\angle ABC| = 60^\circ$ .

### Solution

Draw a rough sketch of the parallelogram.

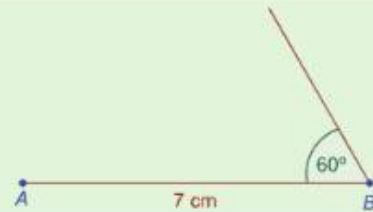


Construct the line segment  $[AB]$  where  $|AB| = 7$  cm.



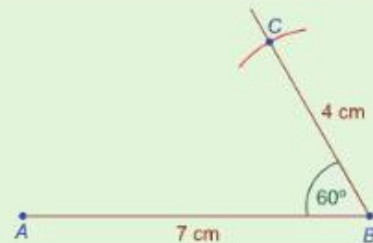
At point  $B$ , construct an angle of  $60^\circ$ , using the line segment  $[AB]$  as one arm of the angle.

Use your protractor for this angle.



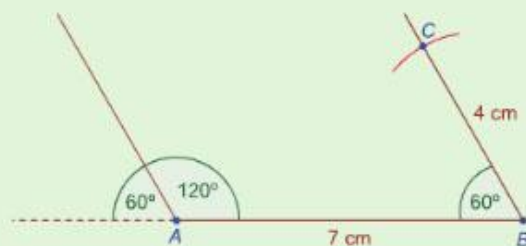
Mark the point  $C$  on this angle such that  $|BC| = 4$  cm.

Use your compass (or ruler) for this measurement.



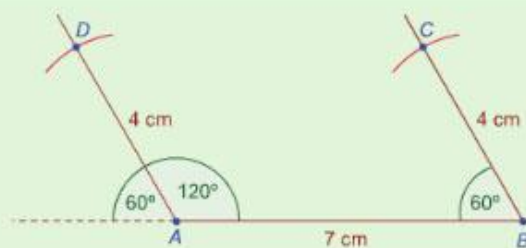
At point  $A$ , construct a ray parallel to  $BC$ .

Use your protractor to measure the correct angle.



Mark the point  $D$  on this ray such that  $|AD| = 4$  cm.

Use your compass (or ruler) for this measurement.



Using a ruler, join  $C$  to  $D$ .

Label all given measurements.

